

Is $x - 2$ a factor of $x^5 - 32$?

If it is, write $P(x)$ as a product of two factors.

$$(2)^5 - 32 = 0$$

$x - 2$ is a factor
 2 is a root

$$\begin{array}{r|rrrrrr} 2 & 1 & 0 & 0 & 0 & 0 & -32 \\ & \downarrow & 2 & 4 & 8 & 16 & 32 \\ \hline & 1 & 2 & 4 & 8 & 16 & 0 \end{array}$$

$$(x-2)(x^4+2x^3+4x^2+8x+16)$$

Use the Factor Theorem to Solve

Solve the equation $2x^3 - 3x^2 - 11x + 6 = 0$
given that 3 is a zero of the function.

$x-3$ is a factor

$$\begin{array}{r} 3 \overline{) 2 \quad -3 \quad -11 \quad 6} \\ \underline{6 \quad 9 \quad -6} \\ 2 \quad 3 \quad -2 \quad \underline{6} \\ 2x^2 + 3x - 2 = 0 \end{array}$$

Roots
 $3, \frac{1}{2}, -2$

$$(2x^2 + 4x)(-x - 2) = 0 \quad \begin{array}{r} -4 \\ -1 \quad \times \quad 4 \\ 3 \end{array}$$

$$2x(x+2) - 1(x+2)$$

$$(2x-1)(x+2)$$

$$x = \frac{1}{2}, -2$$

Solve

$15x^3 + 14x^2 - 3x - 2 = 0$ given that -1 is a zero of the function.

$$\begin{array}{r|rrrr} -1 & 15 & 14 & -3 & -2 \\ & \downarrow & -15 & 1 & 2 \\ \hline & 15 & -1 & -2 & 0 \end{array}$$

$$x = -1, \frac{2}{5}, -\frac{1}{3}$$

Solve

$$f(x) = 3x^3 + 4x^2 + x$$

$$x(3x^2 + 4x + 1) = 0$$

$$x((3x^2 + x) + (3x + 1)) \quad \begin{array}{r} 3 \\ 1 \times 3 \\ \hline 4 \end{array}$$

$$x(x(3x+1) + (3x+1))$$

$$x((x+1)(3x+1)) = 0$$

$$x=0 \quad x+1=0 \quad 3x+1=0$$

$$x=0, -1, -\frac{1}{3}$$