



Products & Factor Theorem  
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Write the function below as a polynomial function in standard form.

FoIL

$$f(x) = (x-1)(x+3)(x+4)$$

$$f(x) = (x^2 + 3x - x - 3)(x+4)$$

$$= (x^2 + 2x - 3)(x+4)$$

$$(x+4)(x^2 + 2x - 3)$$

$$\begin{array}{r} x^3 + 2x^2 - 3x \\ 4x^2 + 8x - 12 \\ \hline \end{array}$$

$$x^3 + 6x^2 + 5x - 12$$

Write the function below as a polynomial function in standard form.

$$f(x) = 2x^2(x-2)(3x+1)(x+5)$$

$$f(x) = (2x^3 - 4x^2)(3x+1)(x+5)$$

$$6x^5 + 20x^4 - 54x^3 - 20x^2$$



Write the function below as a polynomial function in standard form.

$$f(x) = -3x^2(x-2)(2x^2-4x+1)$$

● ● ● | Factor Completely:  
 $x^3 - 16x^2 + 64x$

$$x(x^2 - 16x + 64)$$

$$x(x - 16)(x - 16)$$

① GCF

$$\begin{array}{r} 64 \\ -8 \quad -8 \\ \hline -16 \end{array}$$

● ● ● | Factor Completely:

$$(x^3 + 6x^2 - 5x - 30)$$
$$x^2(x + 6) - 5(x + 6)$$
$$(x^2 - 5)(x + 6)$$

● ● ● | Factor Completely:

$$x^3 - 9x$$

$$\times (x^2 - 9)$$

$$\times (x + 3)(x - 3)$$

● ● ● | Factoring Perfect Cubes

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$



● ● ● | Factor Completely:



$$(x+5)(x^2 - 5x + 25)$$

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● ● ● | Factor Completely:

$$8x^3 - 27$$

$$(2x - 3)(4x^2 + 6x + 9)$$



## Factor Theorem

- $x - r$  is a factor of the polynomial expression that defines the function  $P$  if and only if  $r$  is a solution of  $P(x)=0$ , that is if and only if  $P(\underline{r})=0$ .
- $r$  is a root (zero) iff  $P(r) = 0$

● ● ● Determine whether  $x+3$  is a factor of  $x^3 - 2x^2 - 5x + 6$

$$x+3=0$$

$$x=-3$$

$$(-3)^3 - 2(-3)^2 - 5(-3) + 6$$

$$-27 - 18 + 15 + 6$$

$$-24$$

$\therefore x+3$  is **Not** a factor b/c the answ is not zero

$$\begin{array}{r|rrrr} -3 & 1 & -2 & -5 & 6 \\ & \downarrow & -3 & 15 & -30 \\ \hline & 1 & -5 & 10 & -24 \end{array}$$