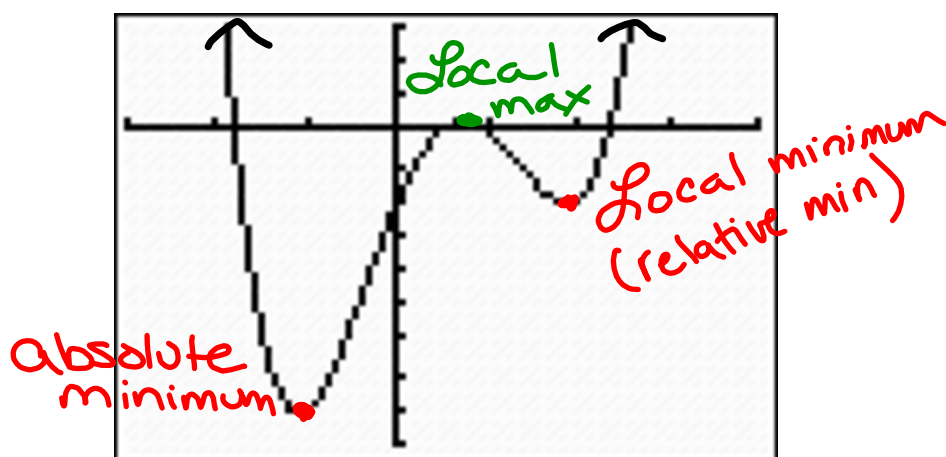


Local Max / Min (in terms of y)
Increasing / Decreasing (in terms of x)



$$f(x) = x^4 - 2x^3 - 3x^2 + 6x - 2$$

$$\begin{aligned} \text{Max} & 0.29 \\ \text{Min} & -8.1 \\ & -2.12 \end{aligned}$$

Turning Points

A polynomial function of degree n has at most $n-1$ turning points.

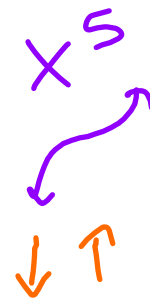
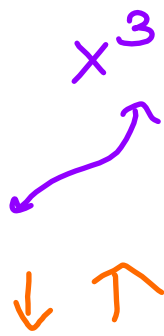
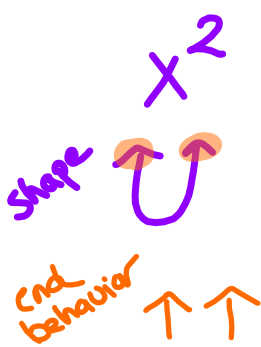
Max #
of turns

4 1. $f(x) = 3x^5 - 4x^3 + 3x^2 + 2$

3 2. $f(x) = x^3 - 3x^4 + 2x^2 - 1$

1 3. $y = x^2 + 2x + 3$





end behavior describes what y is doing

End Behavior of Graphs

"approaches" or "goes to"

$$f(x) \rightarrow \underline{\infty} \text{ as } x \rightarrow +\infty$$
$$f(x) \rightarrow \underline{-\infty} \text{ as } x \rightarrow -\infty$$

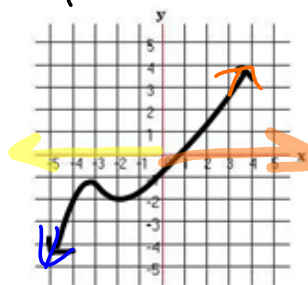
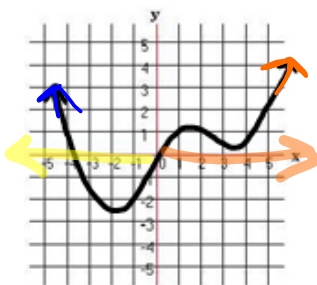
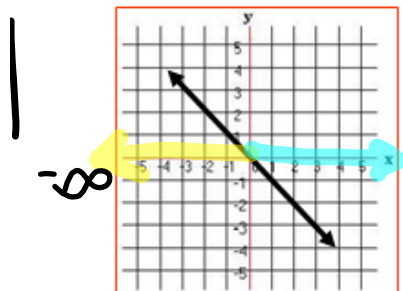
what does y do as x gets bigger and smaller

End Behavior of Graphs

$$f(x) \rightarrow \underline{\hspace{2cm}} \text{ as } x \rightarrow +\infty$$

$$f(x) \rightarrow \underline{\hspace{2cm}} \text{ as } x \rightarrow -\infty$$

$$\left. \begin{array}{l} f(x) \rightarrow -\infty, \text{ as } x \rightarrow \infty \\ f(x) \rightarrow \infty, \text{ as } x \rightarrow -\infty \end{array} \right\} \begin{array}{l} f(x) \rightarrow \infty \text{ as } x \rightarrow \infty \\ f(x) \rightarrow -\infty \text{ as } x \rightarrow -\infty \end{array} \quad \left. \begin{array}{l} f(x) \rightarrow \infty \text{ as } x \rightarrow \infty \\ f(x) \rightarrow -\infty \text{ as } x \rightarrow -\infty \end{array} \right\}$$



End Behavior of Graphs

	+Lead Coefficient	-Lead Coefficient
Even Degree $x^2, x^4, x^6 \dots$	$\uparrow\uparrow$ $f(x) \rightarrow \infty, x \rightarrow \infty$ $f(x) \rightarrow \infty, x \rightarrow -\infty$	$\downarrow\downarrow$ $f(x) \rightarrow -\infty, x \rightarrow \infty$ $f(x) \rightarrow -\infty, x \rightarrow -\infty$
Odd Degree $x^3, x^5, x^7 \dots$	$\downarrow\uparrow$ $f(x) \rightarrow \infty, x \rightarrow \infty$ $f(x) \rightarrow -\infty, x \rightarrow -\infty$	$\uparrow\downarrow$ $f(x) \rightarrow -\infty, x \rightarrow \infty$ $f(x) \rightarrow \infty, x \rightarrow -\infty$



Graphs of Polynomial Functions

- Quadratic: $f(x) = x^2 - 2x$

D: $(-\infty, \infty)$ y-int 0

R: $[-1, \infty)$ $0^2 - 2(0)$

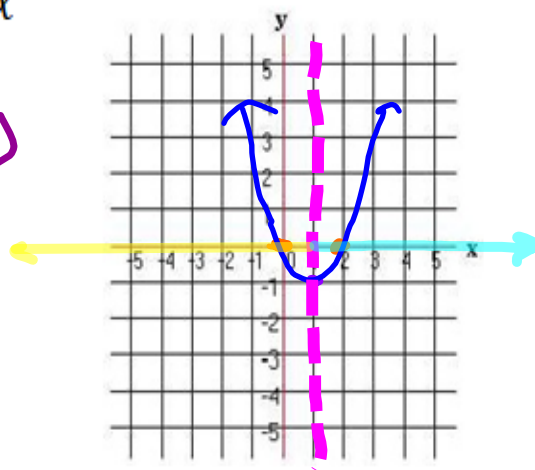
Zeros: 0, 2

Inc: $(1, \infty)$

Dec: $(-\infty, 1)$

as $x \rightarrow \infty, f(x) \rightarrow \infty$

as $x \rightarrow -\infty, f(x) \rightarrow \infty$



Graphs of Polynomial Functions

• Cubic: $f(x) = x^3 + x^2$

D: $(-\infty, \infty)$ y-int 0

R: $(-\infty, \infty)$

Zeros: $-1, 0$

Inc: $(-\infty, -0.67) \cup (0, \infty)$

Dec: $(-0.67, 0)$

as $x \rightarrow \infty, f(x) \rightarrow \infty$

as $x \rightarrow -\infty, f(x) \rightarrow -\infty$

