

● ● ● | Solve:

Factor

$$x^2 + 7x + 10$$

$$(x + 5)(x + 2)$$

2. $(2^4 + 4) \div 5 \times 3 - 7 + 4$

$$(16 + 4) \div 5 \times 3 - 7 + 4$$

$$20 \div 5 \times 3 - 7 + 4$$

$$4 \times 3 - 7 + 4$$

$$12 - 7 + 4$$

$$5 + 4$$

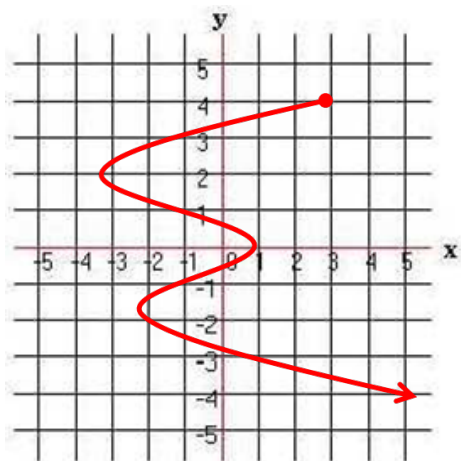
$$\textcircled{9}$$

Operations with Functions 8/10

● ● ● | Function Notation

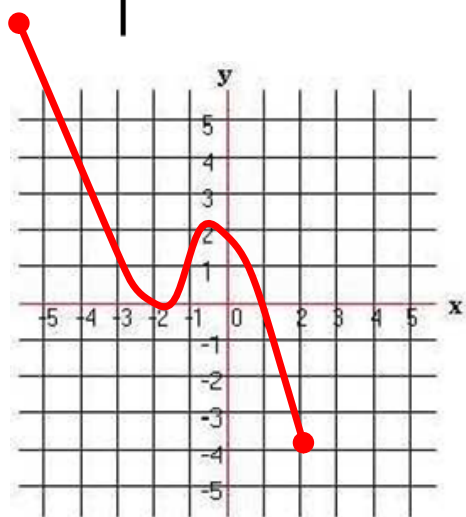


Is it a function? Give the domain and range.



Is the inverse a function?

Is it a function? Give the domain and range.



Is the inverse a function?

Function Notation

● ● ● *function name*

function

$f(x) = 3x^2 - x + 2$

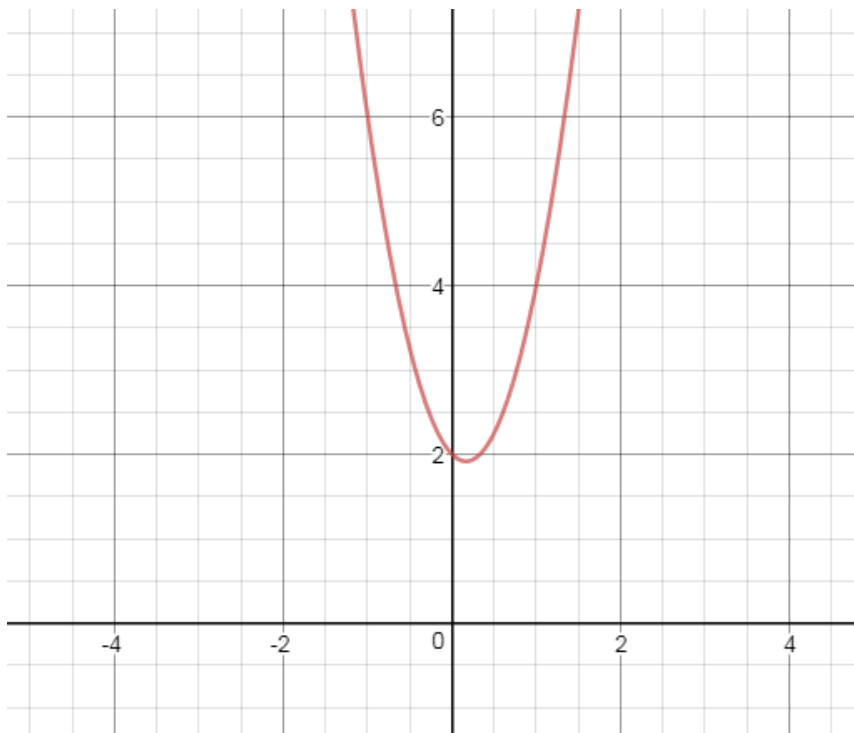
$y = f(x)$ Find: y is a function of x

$$f(-3) = 3(-3)^2 - (-3) + 2 = 32$$

$$f(0) = 2$$

$$f(4)$$

| x | $f(x)$ |
|-----|--------|
| -3 | 32 |



● ● ● | Function Notation

$$f(x) = x^2 - x + 2$$

Find:

$$f(m)$$

$$f(m) = (m)^2 - m + 2$$

$$m^2 - m + 2$$


$$f(m+3)$$

$$f(m+3) = (m+3)^2 - (m+3) + 2$$

$$(m+3)(m+3)$$


$$m^2 + 6m + 9 - m - 3 + 2$$

$$m^2 + 5m + 8$$



Since the value for y depends on what we use for x , we say that....

- Y is the dependent variable
- X is the independent variable



Operations with Functions

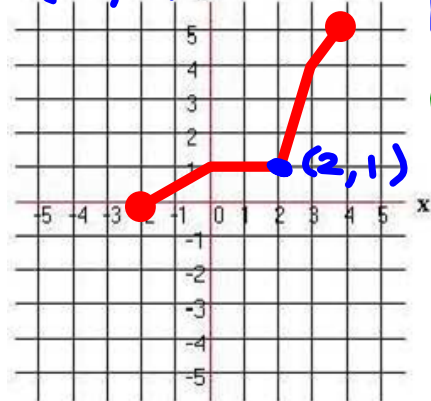


Find:



$$\underline{f(2) + g(4)}$$

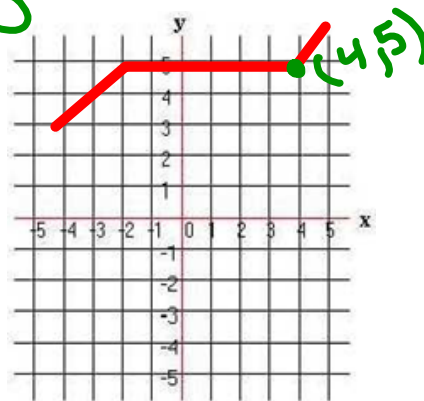
(2,)



$f(x)$

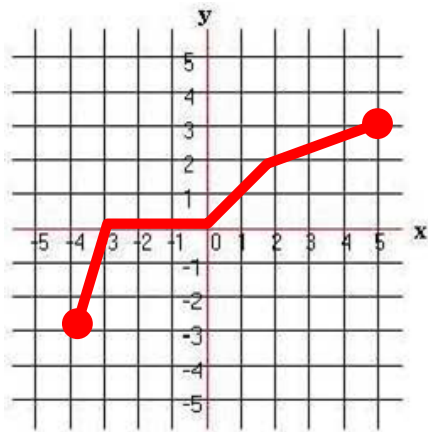
$$1 + 5$$

6

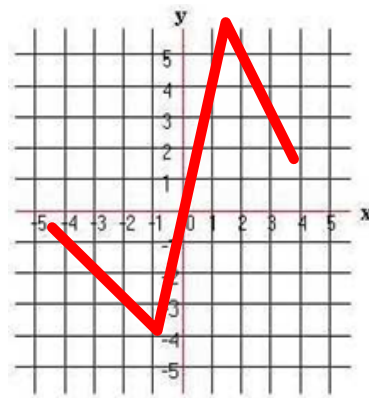


$g(x)$

● ● ● | Find: $f(-1) + g(0)$



$f(x)$



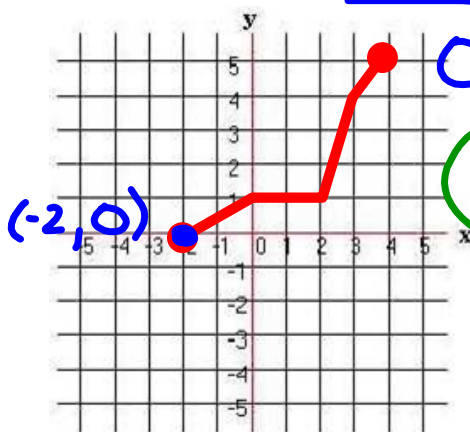
$g(x)$



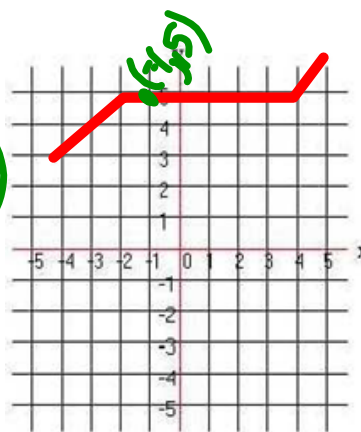
Find:



$$\underline{f(-2)} - g(-1)$$



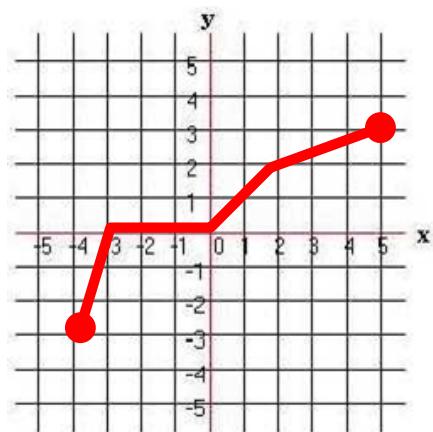
$f(x)$



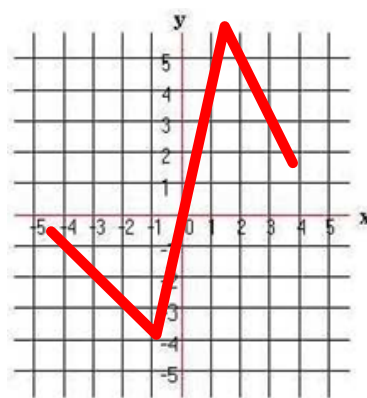
$g(x)$

0 -5
-5

● ● ● | Find: $f(5) - g(0)$



$f(x)$



$g(x)$

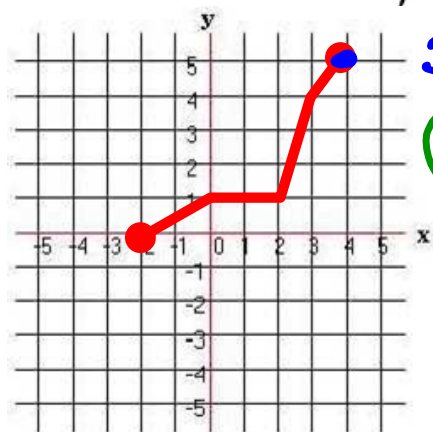


Find:

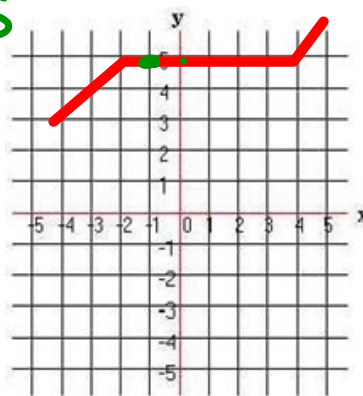


$$f(4) \cdot g(-1)$$

$$5 \cdot 5$$
$$\textcircled{25}$$

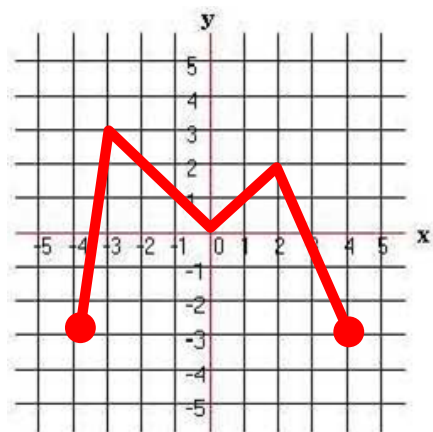


$f(x)$

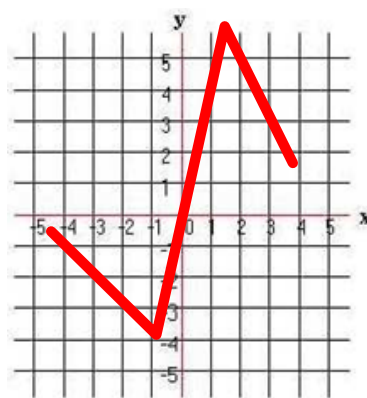


$g(x)$

● ● ● | Find: $f(-4) \cdot g(2)$



$f(x)$

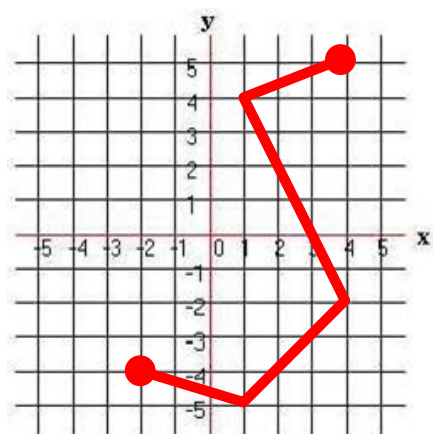


$g(x)$

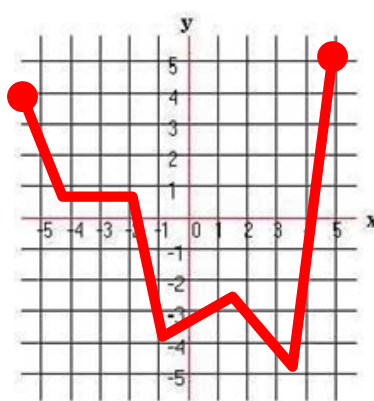


Find:

$$f(-2) \div g(0)$$

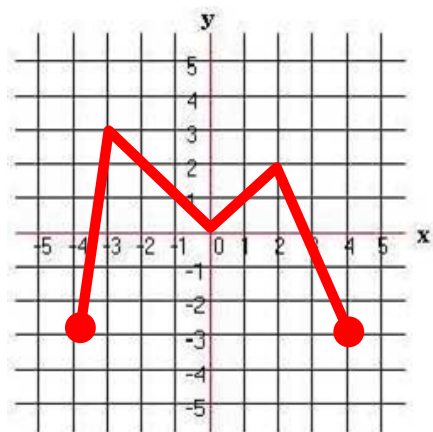


$f(x)$

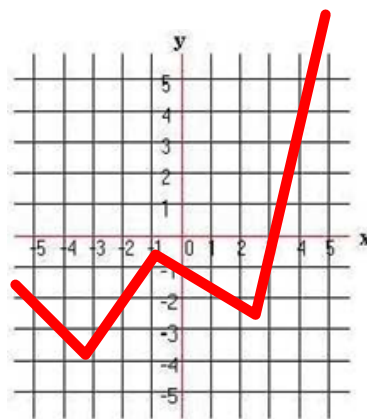


$g(x)$

● ● ● | Find: $g(5) \div f(-3)$



$f(x)$



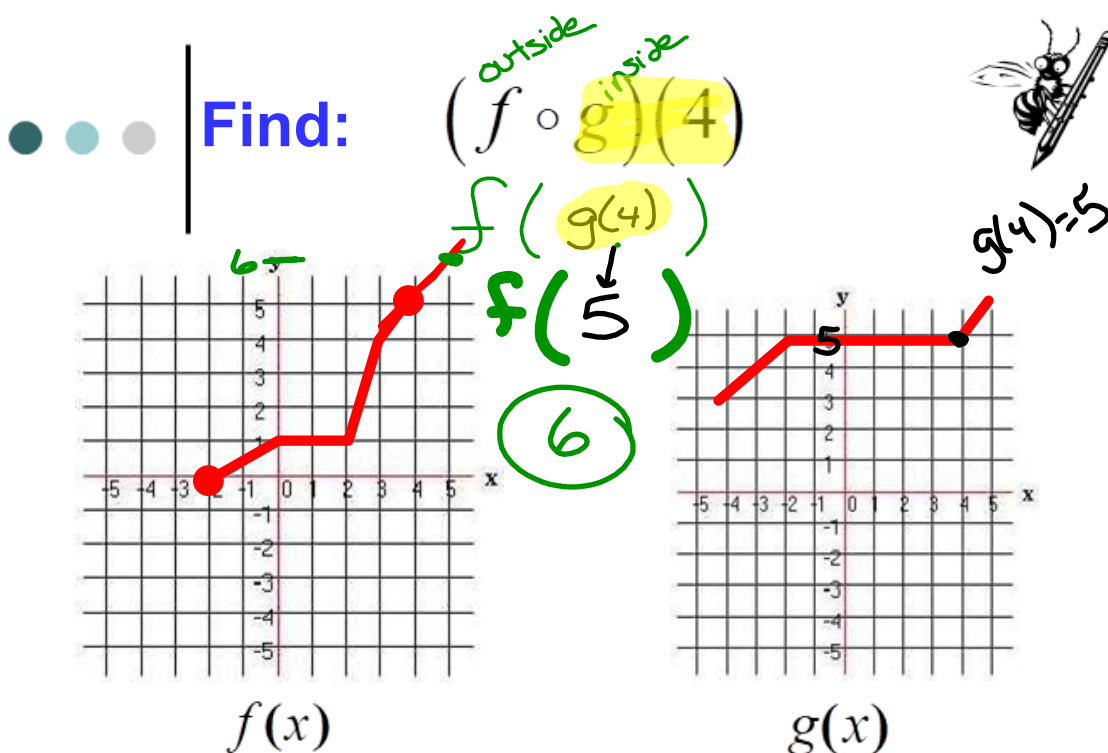
$g(x)$

Compositions with Functions



Plug one function into the other function.

○ open circle

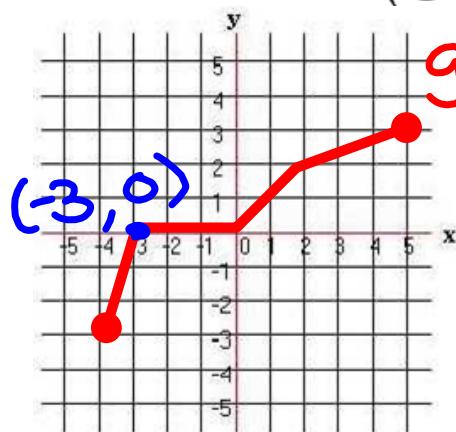




Find:

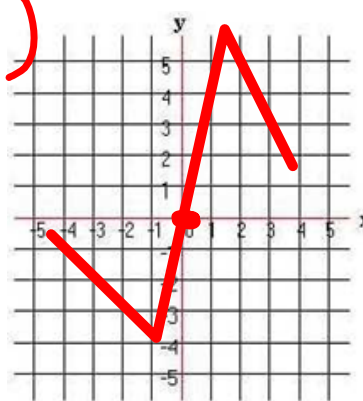


$(g \circ f)(-3)$ $g(f(-3))$



$f(x)$

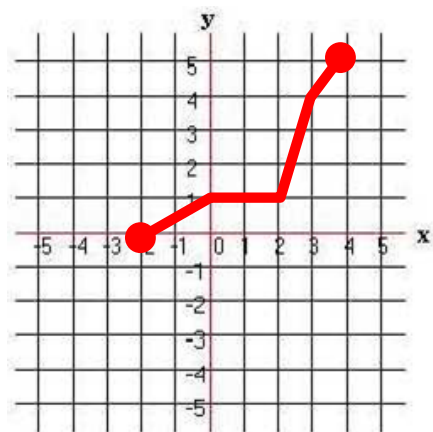
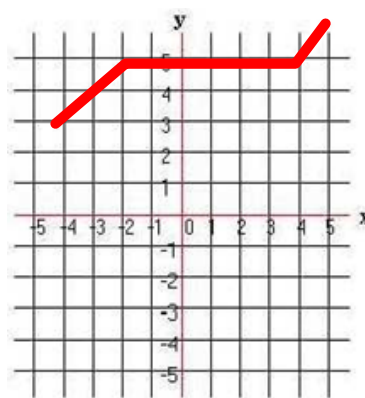
$g(0)$
 0



$g(x)$

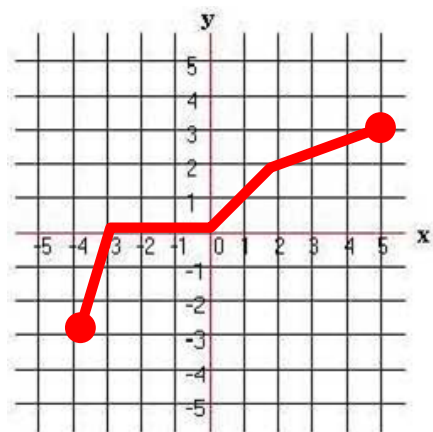
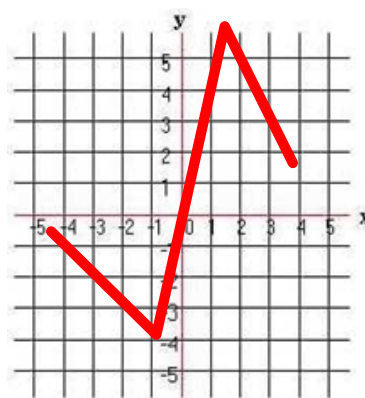
**Find:**

$$f(g(-2))$$

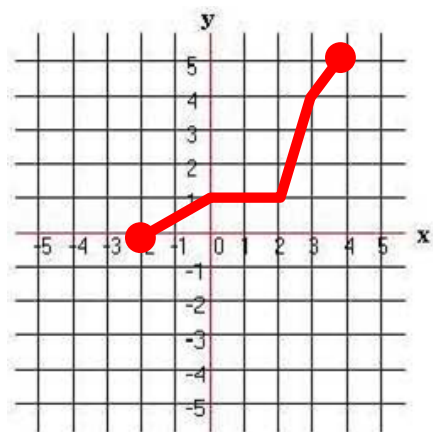
 $f(x)$  $g(x)$

**Find:**

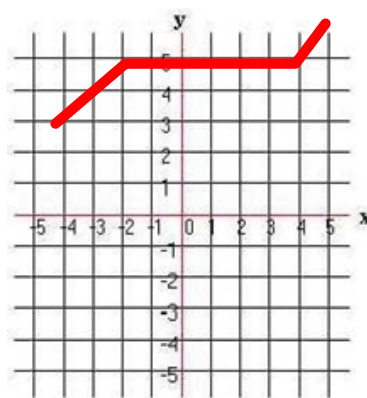
$$f(g(0))$$

 $f(x)$  $g(x)$

● ● ● | Find: $f(f(-2))$



$f(x)$



$g(x)$

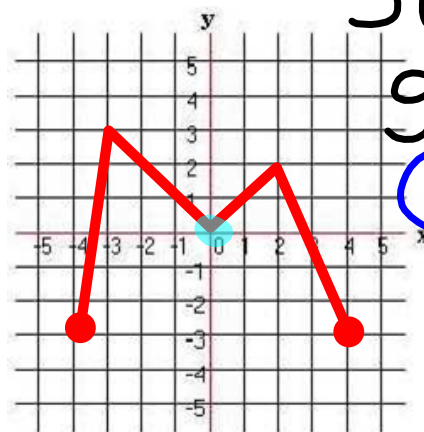


Find:

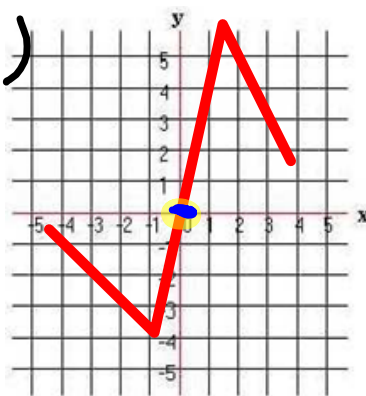
$$g(f(g(0)))$$

$$g(f(0))$$


$$g(0)$$

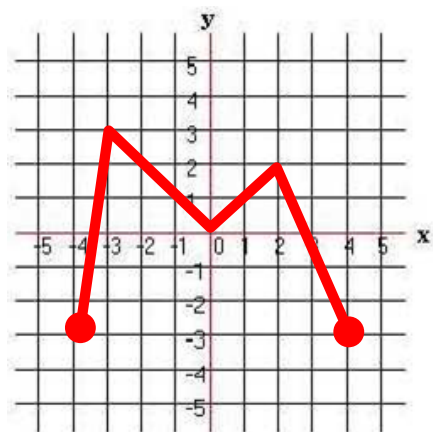
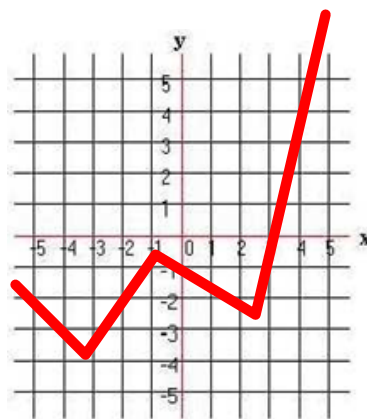


$f(x)$



$g(x)$

● ● ● | Find: $[f \circ g(-2)] - [g \circ f(0)]$ 

 $f(x)$  $g(x)$

Algebraically

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Operations With Functions

Operations

- **Sum:** $(f + g)(x) = f(x) + g(x)$
- **Difference:** $(f - g)(x) = f(x) - g(x)$
- **Product:** $(f \cdot g)(x) = f(x) \cdot g(x)$
- **Quotient:** $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}, \quad g(x) \neq 0$



$$\bullet \bullet \bullet \left| f(x) = x^2 - x + 2 \right.$$

$$\boxed{g(x)} = x^2 + x - 4$$

$$f(x) + g(x)$$

$$(x^2 - x + 2) + (x^2 + x - 4)$$

$$\cancel{x^2} + 2 + \cancel{x^2} + \cancel{x} - 4$$

$$\boxed{2x^2 - 2}$$

$$g(x) + g(x)$$

$$(x^2 + x - 4) + (x^2 + x - 4)$$

$$\boxed{2x^2 + 2x - 8}$$

$$g(x) + f(x)$$

$$\bullet \bullet \bullet \left| \begin{array}{l} \boxed{f(x)} = x^2 + 2x - 3 \\ \boxed{g(x)} = x^2 - 3x + 4 \end{array} \right.$$

 $f(x) - g(x)$

$$\begin{array}{r} (x^2 + 2x - 3) - (x^2 - 3x + 4) \\ \cancel{x^2} + 2x - 3 - \cancel{x^2} + 3x - 4 \end{array}$$

$$\boxed{5x - 7}$$

 $g(x) - f(x)$

$$\dots | \textcircled{f(x)} = 2x - 3$$

$$\textcircled{g(x)} = 3x - 4$$

$$f(x) \cdot g(x)$$

$$(2x - 3)(3x - 4)$$

$$6x^2 - 8x - 9x + 12$$

$$6x^2 - 17x + 12$$

$$\textcircled{f(x)}/g(x)$$

$$\frac{2x - 3}{3x - 4}$$



$$f(x) = 6x - 1$$

$$g(x) = 2x + 3$$

outside \curvearrowright inside

$$(f \circ g)(x) =$$

$$6x - 1$$

$$6(2x + 3) - 1$$

$$12x + 18 - 1$$

$$12x + 17$$

outside \circ inside

$$g \circ f =$$

$$2x + 3$$

$$2(6x - 1) + 3$$

$$12x - 2 + 3$$

$$12x + 1$$

$$\begin{cases} f(x) = x^2 + 4 \\ g(x) = 7x \end{cases}$$



$$(f \circ g)(x) = \begin{matrix} * & \text{outside} & & \text{inside} \\ & & (g \circ f)(-3) = & \end{matrix}$$

$$g(f(-3))$$

$$g(13)$$

$$7(13)$$

$$\textcircled{91}$$

plugged the number into the inside function & Simplified

plugged the answer into the outside function & Simplified

